

Problem 8.2

T & L 3.1

What is $\frac{\epsilon_1}{\epsilon_{\text{total}}}$ where ϵ_1 is due to eddies of size $\lambda \ll \lambda \ll l$

use result from T & L prob. 1.3

$$v(\lambda) \sim (\lambda \epsilon)^{1/3} \sim \left(\lambda \frac{u^3}{l} \right)^{1/3} = u \left(\frac{\lambda}{l} \right)^{1/3}$$

$$\text{but } \lambda/l \sim R_\ell^{-1/2} \sim R_\lambda^{-1} \quad (3.2.17)$$

$$\text{so } v(\lambda) \sim u R_\ell^{-1/6} \sim u R_\lambda^{-1/3}$$

$$\epsilon_{\text{total}} \sim \frac{v u^2}{\lambda^2}, \text{ definition of Taylor microscale}$$

$$\epsilon_1 \text{ due to strain rate } \frac{v_1}{\lambda} \rightarrow \frac{v v_1^2}{\lambda^2} \sim \frac{v u^2 R_\ell^{-1/3}}{\lambda^2}$$

$$\frac{\epsilon_1}{\epsilon_{\text{total}}} \sim R_\ell^{-1/3} \sim R_\lambda^{-2/3} \ll 1 \text{ for large } R_\ell, R_\lambda$$